

HOMEWORK 4
STA701.01, Statistical Inference
Fall Semester, 2013

Due: Tues Oct 1st, 2013

- 1 If we have a finite \mathcal{S} , then show that a minimax rule always exists.
- 2 Let $X_1, \dots, X_n \sim N(\mu, \sigma^2)$. Show that \bar{X} and s^2 are unbiased estimators for μ and σ^2 , respectively.
- 3 Let $X_1, \dots, X_n \sim \text{Bernoulli}(p)$. Let $Y = \sum_{i=1}^n X_i$. Let $\hat{p}_1 = Y/n$ and $\hat{p}_2 = (Y + \alpha)/(\alpha + \beta + n)$ where $\alpha = \beta = \sqrt{n/4}$. Consider the squared error loss and risks

$$R(p, \hat{p}_1) = \frac{p(1-p)}{n}$$

and

$$R(p, \hat{p}_2) = \frac{n}{4(n + \sqrt{n})^2}.$$

Plot $R(p, \hat{p}_1)$ and $R(p, \hat{p}_2)$. What can you say about them?