

STA 624.01
Applied Stochastic Processes
Spring Semester, 2007
Monday Wednesday Friday 12:00 PM–12:50 PM
Room CB 307

Instructor: Ruriko Yoshida
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Office hours: Monday Wednesday 10:00-11:00 AM
(I'm usually available to talk whenever I'm in my office so
feel free to drop in, except two minutes before class starts.)
Text: "Introduction to Stochastic Processes" Lawler

Overview: This is a course on stochastic processes, which involve collections of random variables indexed by time or by space. In this course you will learn the nomenclature and techniques needed for understanding the major types of stochastic processes, how to apply these processes in mathematical modeling, and how to effectively compute and simulate using these processes. We will cover materials including (not limited to) discrete-time and continuous-time Markov Chain, Reversible Markov Chain, hidden Markov Model (HMM). For computing I will be teaching the basics of MATLAB, although you may utilize any environment you are familiar with for completing the assignments.

Course Website: All course materials (including the homework assignments) will be posted on the class website, which you can access using the Blackboard system found at

<https://www.ms.uky.edu/~ruriko/courses/Stat624S07/>

Homework: Assignments will be weekly, handed out on Friday and due back the next Friday. Typically these assignments contain 4 or 5 regular problems and one computer problem.

While you are welcome to work together on the assignments, the final writeups should be your own. In the writeups, indicate your calculations and reasoning for all the work submitted. For numerical answers, draw a box around your answer and use four significant figures for approximations unless the answer is an integer, or instructed otherwise in the problem statement.

Homework will be graded on a ten point scale 0 meaning that you did not turn in the homework and 10 meaning that Athena, goddess of wisdom could not have completed the assignment any better. You will receive two scores, one for the regular problems and one for the computer work. **ABSOLUTELY NO LATE homework.**

Before handing in your homework paper, please staple all papers together and clearly write your name and the assignment number on the first page. Turn in papers held together by paper clips or origami at your own risk.

The lowest homework score of each semester will be thrown out. This is basically to handle those emergencies where you are unable to complete an assignment for external reasons. I strongly recommend you save this freebie as long as possible and do not blow off an early assignment.

Tests: There will be 2 midterms during the semester, both in class. They will test your ability to recall key definitions and theorems from the class, and apply them to simple problems. In addition, there will be a final exam roughly twice the length of the midterms.

Grading: The regular problems of the homework are worth 20% of your grade, the computer problems 15%, midterm 1 is 20%, midterm 2 is 20%, and the final will be 25%.

Schedule: The following is a tentative schedule. It might be changed.

| Week | Topic | Section |
|--|---------------------------------------|---|
| Jan 10 Jan 12 | Basic Probability | Handout |
| Jan 15 | No class | |
| Jan 17 | Matlab Tutorial | Some Matlab Tutorial and Finite Markov Chain |
| Jan 19 Jan 22 Jan 24 Jan 26 Jan 29 Jan 31 | Finite Markov Chains | Examples (1.1) Large time behavior (1.2) Classification of states (1.3) Classification of states (1.3) Return time and Transient States (1.4 – 1.5) Return time and Transient States (1.4 – 1.5) |
| Feb 2 Feb 5 Feb 7 Feb 9 Feb 12 | Countable Markov Chains | Introduction (2.1) Recurrence and Transience (2.2) Recurrence and Transience (2.2) Positive Recurrence and Null Recurrence (2.3) Branching Process (2.4) |
| Feb 14 Feb 16 Feb 19 Feb 21 Feb 23 | Continuourous-time Markov Chains | Poisson Process (3.1) Finite State Space (3.2) Finite State Space (3.2) Birth and Death Process (3.3) Birth and Death Process (3.3) |
| Feb 26 Feb 28 March 2 March 5 | Reversible Markov Chains | Reversible Processes (7.1) Convergence to Equibirium (7.2) Markov Chain Algorithms (7.3) Criterion for Recurrence (7.4) |
| March 7 March 9 | Review First MT | |
| March 18 March 20 March 22 March 25 March 27 | Optimal Stopping | Optimal Stopping of Markov Chains (4.1) Optimal Stopping of Markov Chains (4.1) Optimal Stopping with Cost (4.2) Optimal Stopping with Cost (4.2) Optimal Stopping with discounting (4.3) |
| March 29 April 2 April 4 April 6 April 9 April 11 | Renewal Processes | Introduction (6.1) Introduction (6.1) Renewal Equations (6.2) Discrete Renewal Processes (6.3) Discrete Renewal Processes (6.3) M/G/1 and G/M/1 Queues (6.4) |
| April 13 | Hidden Markov Model (HMM) | |
| April 16 April 18 April 20 | Review Second MT No class | |
| April 23 April 25 | Applications to computational biology | Evolutional models Applications of HMM to computational biology |
| April 27 Aprill 30 | Review (two hours) Final | 1 PM in class |